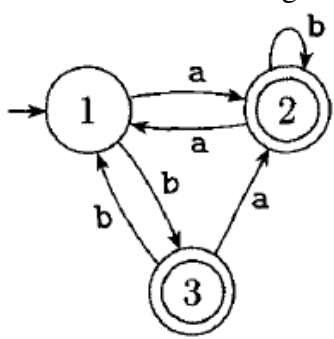


**EVEN SEMESTER EXAMINATION, 2023 – 24**  
**2<sup>nd</sup> yr B.Tech. –Computer Science&Engineering**  
**FORMAL LANGUAGES & AUTOMATA THEORY**

Duration: 3:00 hrs

Max Marks: 100

*Note: - Attempt all questions. All Questions carry equal marks. In case of any ambiguity or missing data, the same may be assumed and state the assumption made in the answer.*

Q 1.	<p>Answer any four parts of the following.</p> <p>a) Give DFAs that recognize the following languages:  <math>\{w \in \{0,1\}^* \mid w \text{ contains } 110 \text{ as a substring}\}</math></p> <p>b) Convert the following Deterministic Finite Automata into Regular Expression.</p>  <pre> graph LR     start(( )) --&gt; 1((1))     1 -- a --&gt; 2(((2)))     2 -- a --&gt; 1     2 -- b --&gt; 2     1 -- b --&gt; 3(((3)))     3 -- a --&gt; 2     style start fill:none,stroke:none   </pre> <p>c) Give context-free grammars having two variables generating the following languages over the alphabet <math>\{a,b\}</math>  <math>L = \text{"The set of strings with more a's than b's"}</math></p> <p>d) State whether the statement is true or false and Briefly give reason in support of your answer. "The class of context-free languages is closed under intersection".</p> <p>e) Discuss four closure properties of Regular Languages and prove that the Regular Languages are closed under them.</p> <p>f) What is Pumping Lemma for regular Language.</p>	5x4=20
Q 2.	<p>Answer any four parts of the following.</p> <p>(a) Put the following grammar into Chomsky Normal Form.  <math>S \rightarrow T \mid TaS</math>  <math>T \rightarrow aTb \mid bTa \mid TT \mid \epsilon</math></p> <p>b) Give DFAs that recognize the following languages:  <math>\{w \in \{0,1\}^* \mid w \text{ contains at least two 0's}\}</math></p> <p>c) State whether the statement is true or false and Briefly give reason in support of your answer: "A context free grammar <math>G</math> and <math>w</math> be a string in <math>L(G)</math>, then the number of leaves in a parse tree of <math>w</math> with respect to <math>G</math> can be more than the length of <math>w</math>".</p>	5x4=20

	<p>d) Construct a Deterministic finite automaton to accept the set <math>L</math> of all strings over <math>\{0,1\}</math> ending with 010.</p> <p>e) Differentiate between Non deterministic finite automata (NFA) and deterministic finite automata(DFA).</p> <p>f) What are regular expressions? Discuss in brief operators of regular expression and their precedence</p>	
Q 3.	<p>Answer any two parts of the following.</p> <p>a) Design a non-deterministic pushdown automata <math>M</math> that recognizes the language <math>L = \{ ww^R \mid w \in \{0,1\}^* \}</math>, where <math>w^R</math> means written backwards. Give the informal description of the PDA.</p> <p>b) Design a Turing machine with no more than three states that accepts the language <math>L(a(a+b)^*)</math>. Assume that <math>\Sigma = \{a,b\}</math>. Is it possible to do this with a two state machine?</p> <p>c) Elaborate Chomsky and Greibach normal forms.</p>	10x2= 20
Q 4.	<p>Answer any two parts of the following.</p> <p>a) Design a Turing machine that copies strings of 1's. More precisely, find a machine that performs the computation. Give the pseudocode of the design.  <math>q_0w \vdash^{**} q_f ww</math>.</p> <p>b) Complete the following state transition diagram of Push Down Automata <math>M</math> that recognizes  <math>L = \{ a^i b^j c^k \mid i,j,k \geq 0 \text{ and } i=j \text{ or } i=k \}</math></p> <pre> graph LR     q1((q1)) -- "ε, ε → \$" --&gt; q2((q2))     q2 -- "a, ε → a" --&gt; q2     q2 -- "ε, ε → ε" --&gt; q5((q5))     q2 -- "ε, ε → a" --&gt; q3((q3))     q3 --&gt; q3     q3 --&gt; q4(((q4)))     q5 --&gt; q5     q5 --&gt; q6((q6))     q6 --&gt; q6     q6 --&gt; q7(((q7)))   </pre> <p>c) What are Recursive languages? Discuss the Properties of recursive languages.</p>	10x2= 20
Q 5.	<p>Answer any two parts of the following.</p> <p>a) Find a grammar having single variable that generates the following language:  <math>L = \{ a^n b^{n+1} \mid n \geq 0 \}</math>          Give the complete specification of the grammar. Construct parse tree for any two strings <math>w \in L</math> and <math> w =5</math>. Show whether the grammar is ambiguous?</p> <p>b) Discuss Undecidable Problems about Turing Machines.</p> <p>c) Design a Turing Machine to recognize all the strings consisting of an even number of 1's. Give the idea of construction and transition table for the Turing machine.</p>	10x2= 20